# Conformational Analysis of 2- and 3-Phosphoglyceric Acids by ${ }^{1} \mathrm{H}$ and ${ }^{13} \mathrm{C}$ Nuclear Magnetic Resonance Spectroscopy 

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#### Abstract

The staggered rotamer populations about the $\mathrm{C}(2)-\mathrm{C}(3)$ and $\mathrm{C}-\mathrm{O}$ (phosphate) bonds of 2 - and 3 -phosphoglyceric acids (2PPG and 3PPG) have been estimated as a function of pH from ${ }^{1} \mathrm{H}-{ }^{1} \mathrm{H},{ }^{1} \mathrm{H}-{ }^{31} \mathrm{P},{ }^{13} \mathrm{C}-1 \mathrm{H}$, and ${ }^{13} \mathrm{C}-{ }^{31} \mathrm{P}$ vicinal coupling constants. For 2PPG in the pH range $5.0-10.8$, between four and five conformations of the molecule may be significantly populated ( $\geqslant 10 \%$ ). For 3PPG at low pH that conformer with the planar trans-arrangement of the $\mathrm{C}(2)-\mathrm{H}$ and $\mathrm{O}-\mathrm{P}$ bonds predominates and is possibly stabilised by intramolecular hydrogen bonding. At higher pH (9.8) there is an increasingly important contribution from that conformer with the $\mathrm{C}(2)-\mathrm{CO}_{2}{ }^{-}$and $\mathrm{O}-\mathrm{PO}_{3}{ }^{2-}$ bonds in a planar trans-arrangement, and this conformer may be stabilised by a combination of intramolecular hydrogen bonding and the electrostatic interaction.


The substances 2-phosphoglyceric acid (2PPG) (I) and 3 -phosphoglyceric acid (3PPG) (II) are important intermediates in the enzyme-catalysed process of glycolysis. In glycolysis a sugar (e.g. D-glucose) is converted to lactate via 3 PPG and 2 PPG , with a high proportion of the overall free-energy decrease being conserved as the phosphate bond energy of adenosine triphosphate (ATP). Our interest lies in the reversible conversion of 3 PPG to

(I)

(II)

2PPG which is catalysed by the enzymes phosphoglyceromutase. The equilibrium constant for this reaction has been measured by Britton and his coworkers ${ }^{1}$ and found to be in the region $8.6-11.7(\mathrm{pH}$ 5.4-8.1) in favour of 3PPG. An anomalous temperature dependence of the equilibrium constant was tentatively ascribed ${ }^{1}$ to more extensive internal hydrogen bonding in 2 PPG relative to 3 PPG, limiting internal mobility in the former. Since n.m.r. spectroscopy is known to be a powerful tool in the elucidation of molecular conformations we have undertaken a study of 2 PPG and 3 PPG using this technique. In the absence of enzyme the rate for equilibration of 2 PPG and 3 PPG is slow on the n.m.r. time scale at all pH values employed in this study.

The Conformations about the $\mathrm{C}(2)-\mathrm{C}(3)$ Bond.Feeney and his co-workers ${ }^{2}$ have detailed a method for estimating rotamer populations about the $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bond in amino-acids by measurement of the vicinal ${ }^{1} \mathrm{H}-{ }^{1} \mathrm{H}$ and ${ }^{13} \mathrm{C}-{ }^{1} \mathrm{H}$ coupling constants. This method is readily applicable to 2 PPG and 3 PPG to investigate conformations about the $\mathrm{C}(2)-\mathrm{C}(3)$ bond. The idealised staggered rotamers whose populations $\left(P_{i}\right)$ are to be estimated are shown in Figure 1, and the conformation-dependent coupling constants are $\mathrm{H}_{\mathrm{A}}-\mathrm{H}_{3}, \mathrm{H}_{\mathrm{B}}-\mathrm{H}_{\mathrm{H}}, \mathrm{C}(1)-\mathrm{H}_{\mathrm{A}}$, and $\mathrm{C}(\mathbf{1})-\mathrm{H}_{\mathrm{B}}$. Since the rotamer populations will depend upon the ionisation state of the phosphate and carboxy-
groups, the analyses of the ${ }^{1} \mathrm{H}$ n.m.r. spectra were performed on samples at pH 5.0 and 10.8 for 2 PPG and pH $0.6,1.0,2.8,4.7$, and 9.8 for 3 PPG.

The species involved in the dissociation equilibria are

(la)

(Ib)

(Ic)

(IIb)

(Da)

(IIC)

Figure 1 Staggered rotamers about $C(2)-C(3)$ available to $\mathrm{D}-(+)-2 \mathrm{Pl}^{\prime} \mathrm{G}$ and $\mathrm{D}-(-)-3 \mathrm{PPG}$
illustrated in the Scheme (the $\mathrm{p} K_{\mathrm{i}}$ are taken from the literature ${ }^{3}$ ).
Typically (see Figure 2) in the cases most suitable for analysis, the ${ }^{1} \mathrm{H}$ spectra of 2 PPG and 3 PPG were second
order showing 24 resonances characteristic of the ABM part of an ABMX spectrum (the X nucleus being ${ }^{31} \mathrm{P}$ ). The splittings due to the ${ }^{31} \mathrm{P}$ nucleus were readily identified from the 12 -line ${ }^{1} \mathrm{H}$ spectra (at 100 MHz ) employing
that of the methine proton $\left(\mathrm{H}_{M}\right)$ is to highest frequency (lowest field) while of the methylene group resonances those due to $\mathrm{H}_{\mathrm{A}}$ have been arbitrarily assigned to lower frequency than $\mathrm{H}_{\mathrm{R}}$ in most cases. For 3PPG at $\mathrm{pH}<$



SCheme $\mathrm{p} K_{1} \simeq 2, \mathrm{p} K_{2}=3.6, \mathrm{p} K_{3}=7.0$ for 2 PPG; $\mathrm{p} K_{1} \simeq 2, \mathrm{p} K_{2}=3.6, \mathrm{p} K_{3}=6.8$
${ }^{31} \mathrm{P}$ decoupling (at 40.5 MHz$) .{ }^{1} \mathrm{H}-\left({ }^{31} \mathrm{P}\right)$ Spectra of 2 PPG at $\mathrm{pH}<5$ were deceptively simple ${ }^{4}$ yielding less than 12 lines and were not suitable for full analysis of


Figure $2 \quad 360 \mathrm{MHz}{ }^{1} \mathrm{H}$ Spectrum of 3 PPG at pH 0.6 :
(a) experimental spectrum, (b) calculated spectrum
the inter-proton couplings. The coupling constants obtained by analysis (see Experimental section) of the ${ }^{1} \mathrm{H}$ spectra are collected in Table 1 together with the ${ }^{1} \mathrm{H}$ chemical shifts. Of the three groups of ${ }^{1} \mathrm{H}$ resonances,
$2.8, \mathrm{H}_{\mathrm{B}}$ has been assigned to lower frequency than $\mathrm{H}_{\mathrm{A}}$. This seems reasonable since the $\mathrm{H}_{\mathrm{A}}-\mathrm{H}_{\mathrm{B}}$ chemical shift separation is a minimum at pH 2.8 (Table 1) and this proposed cross-over in chemical shifts avoids a switch in the relative magnitudes of $J_{\mathrm{AM}}$ and $J_{\mathrm{BM}}$ (and subsequently in $P_{\text {IIa }}$ and $P_{\text {IIc }}$ ) and in $J_{\mathrm{AP}}$ and $J_{\mathrm{BP}}$ in the pH region $1.0-2.8$. In addition the consequences of the cross-over are reasonable on chemical grounds (see Discussion).

Because of rapid rotation about the $\mathrm{C}(2)-\mathrm{C}(3)$ bond for both 2 PPG and 3 PPG, the vicinal couplings in Table i are values averaged over the three rotamers. In order to further analyse the vicinal couplings in terms of the rotamer populations, ${ }^{2}$ values for the trans-vicinal coupling [ ${ }^{3} J_{\mathrm{AM}}$ in rotamer (Ia), Figure 1] and the gauche $\left[{ }^{3} J_{\mathrm{AM}}\right.$ in rotamer (Ib), Figure l] must be obtained from model systems wherein the pattern of substituents about the $\mathrm{C}-\mathrm{C}$ bond is as similar as possible to 2 PPG and 3 PPG . Such a model is $3^{\prime}, 5^{\prime}$-cyclic thymidine monophosphate (III) from which values for the trans $\left({ }^{3} J_{\mathrm{HH}}{ }^{t}\right)$ and gauche ${ }^{3} J_{\mathrm{HH}}{ }^{g}$ ) vicinal couplings between the protons at $\mathrm{C}\left(4^{\prime}\right)$ and $C\left(5^{\prime}\right)$ have been measured ${ }^{5}$ to be 10.1 and 2.1 Hz , respectively.

Table 1
${ }^{1} \mathrm{H}-{ }^{1} \mathrm{H}$ and ${ }^{1} \mathrm{H}-{ }^{31} \mathrm{P}$ coupling constants ${ }^{a}$ and chemical shifts ${ }^{b}$ for 2PPG and 3PPG

|  |  |  | 2 PPG |  |  |  |  | 3 PPG |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | pH | 1.0 | 2.8 | 5.0 | 10.8 | 0.6 | 1.0 | 2.8 | 4.7 | 9.8 |
| ${ }^{3}{ }^{\text {J AM }}$ |  | $\left\|7.0_{3}\right\|^{\text {b }}$ | $\mid 7.48{ }^{\text {b }}$ | 5.00 | 5.44 | 4.16 | 4.30 | 5.49 | 5.87 | 6.15 |
| ${ }^{3} J_{\text {BM }}$ |  |  |  | 3.07 | 2.94 | 3.06 | 3.12 | 2.38 | 2.61 | 2.75 |
| ${ }^{2} J_{\text {AB }}$ |  | $-12.47$ |  | $-12.13$ | $-11.7{ }_{4}$ | $-10.90$ | $-10.96$ | $-10.9{ }_{6}$ | $-10.7_{9}$ | $-11.0{ }_{6}$ |
| ${ }^{3}{ }^{3}$ MP |  | 9.48 | 9.28 | 8.87 | 8.6 |  |  |  |  |  |
| ${ }^{3} J_{\text {AP }}$ |  |  |  |  |  | 6.47 | 6.49 | 6.22 | 5.64 | 5.94 |
| ${ }^{3}{ }^{4} \mathrm{BP}$ |  |  |  |  |  | 5.17 | 5.0 | 5.02 | 5.25 | 5.91 |
| ${ }^{4} J_{\text {MP }}$ |  |  |  |  |  | 1.77 | 1.59 | $1.3{ }_{6}$ | 1.23 | 0.57 |
| $\delta_{\text {A }}$ |  | $4.47{ }_{6}$ | $4.42{ }_{6}$ | $4.36{ }_{6}$ | 4.305 | 4.727 | $4.67{ }_{4}$ | $4.59{ }_{4}$ | $4.47{ }_{4}$ | $4.38{ }_{8}$ |
| $\delta_{\text {B }}$ |  | $4.45{ }_{8}$ | $4.42{ }_{6}$ | $4.40{ }_{9}$ | $4.40{ }_{7}$ | $4.72{ }_{7}$ | $4.67{ }_{4}$ | $4.59_{4}$ | $4.47{ }_{4}$ | $4.38{ }^{\text {g }}$ |
| $\delta_{M}$ |  | 5.247 | $5.13{ }_{3}$ | $5.00{ }_{4}$ | $4.96{ }_{4}$ | $5.04{ }_{2}$ | $5.0 \mathrm{I}_{2}$ | 4.893 | 4.69 | $4.69{ }_{6}$ |

a Coupling constants in Hz ; chemical shifts in p.p.m. to high frequency of external $\mathrm{Me}_{4} \mathrm{Si}$, from analysis of $360-\mathrm{MHz}{ }^{1} \mathrm{H}$ spectra; labelling of protons as in Figure 1. ${ }^{6}$ Only the sum ${ }^{3} J_{A M}+{ }^{3} J_{B M}$ can be calculated from these deceptively simple ${ }^{1} \mathrm{H}$ spectra.

The equations relating the rotamer populations to the vicinal couplings have been given by Feeney et al., ${ }^{2}$ and applied to 2 PPG are of the form (1); these equations

$$
\begin{align*}
J_{\mathrm{AM}} & =P_{\mathrm{Ia}} J_{\mathrm{HH}}{ }^{t}+P_{\mathrm{Ib}} J_{\mathrm{HH}}^{g}+P_{\mathrm{Ic}} J_{\mathrm{HH}^{g}} \\
J_{\mathrm{BM}} & =P_{\mathrm{Ia}} J_{\mathrm{HH}^{g}}+P_{\mathrm{Ib}} J_{\mathrm{HH}}+P_{\mathrm{Ic}} J_{\mathrm{HH}^{t}} \\
1 & =P_{\mathrm{Ia}}+P_{\mathrm{Ib}}+P_{\mathrm{Ic}} \tag{I}
\end{align*}
$$

may be solved for the rotamer populations $P_{i}$. However, because of the ambiguity in the assignment of the resonances due to $\mathrm{H}_{\mathrm{A}}$ and $\mathrm{H}_{\mathrm{B}}$ the values obtained for $P_{\text {Ia }}$ and $P_{\text {Ic }}$ may be interchanged. The values calculated for the rotamer populations are given in Table 2.

(II)

The uncertainty is removed by consideration ${ }^{2}$ of the vicinal ${ }^{13} \mathrm{C}^{-1} \mathrm{H}$ couplings at $\mathrm{C}(\mathrm{l})$. This procedure may be understood if we consider the two solutions (2) and (3)

$$
\begin{align*}
& P_{\mathrm{Ia}}=l, P_{\mathrm{Ib}}=m, P_{\mathrm{Ic}}=n  \tag{2}\\
& P_{\mathrm{Ia}}=n, P_{\mathrm{Ib}}=m, P_{\mathrm{Ic}}=l \tag{3}
\end{align*}
$$

$J_{\mathrm{C}(\mathbf{1}) \mathrm{H}_{\mathrm{A}}}+J_{\mathrm{C}(\mathbf{1}) \mathrm{H}_{\mathrm{B}}}=(2 l+m+n) J_{\mathrm{CH}^{g}}+$

$$
\begin{equation*}
(m+n) J_{\mathrm{CH}^{t}} \tag{4}
\end{equation*}
$$

$J_{\mathrm{C}(1) \mathrm{H}_{\mathrm{A}}}+J_{\mathrm{C}(1) \mathrm{H}_{\mathrm{B}}}=(l+m+2 n) J_{\mathrm{OH}^{g}}+$

$$
\begin{equation*}
(l+m) J_{\mathrm{CH}^{t}} \tag{5}
\end{equation*}
$$

for the $P_{i}$. If solution (2) is true then (Figure 1 ), then equation (4) holds, or if solution (3) is true, equation (5),
carbon of (IV) yielded ${ }^{2} J_{\mathrm{CH}^{g}}+J_{\mathrm{CH}^{t}}=11.1 \mathrm{~Hz}$. The coupling constants at $\mathrm{C}(1)$ taken from the analysis*

(IV)
of the single-resonance ${ }^{13} \mathrm{C}$ spectra of 2 PPG and 3 PPG are given in Table 3. Using the rotamer populations

Table 2
Rotamer populations ${ }^{a}$ for 2PPG $\left(P_{\mathrm{II} i}\right)$ and 3 PPG ( $P_{\mathrm{II} i}$ )

|  | pH | 1.0 | 2.8 | 5.0 | 10.8 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | Bond |
| $P_{\text {Ia }}$ |  |  |  | 0.36 | 0.42 |  |
| $P_{\text {lb }}$ |  |  |  | 0.52 | 0.47 | $\underset{\mathrm{C}(3)-}{\mathrm{C}(2)}$ |
| $P_{\text {Ic }}$ |  |  |  | 0.12 | 0.11 |  |
| $P_{\text {Id }}$ |  | 0.27 | 0.27 | 0.25 | 0.24 | $\mathrm{O}-\mathrm{C}(2)$ |
| $P_{\text {fe }}$ |  | 0.27 | 0.27 | 0.29 | 0.60 |  |
| $P_{\text {If }}$ |  | 0.46 | 0.46 | 0.46 | 0.16 |  |
|  | pH | 0.6 | 1.0 | 2.8 | 4.7 | 9.8 |
| $P_{\text {IIa }}$ |  | 0.26 | 0.28 | 0.42 | 0.47 | 0.51 |
| $P_{\text {IIb }}$ |  | 0.62 | 0.59 | 0.54 | 0.47 | $\begin{array}{cc} 0.41 & \mathrm{C}(2)- \\ & \mathrm{C}(3) \end{array}$ |
| $P_{\text {HIE }}$ |  | 0.12 | 0.13 | 0.04 | 0.06 | 0.08 |
| $P_{\text {IId }}$ |  | 0.73 | 0.74 | 0.75 | 0.77 | 0.73 |
| $P_{\text {Ile }}$ |  | 0.16 | 0.16 | 0.15 | 0.12 | $0.14 \mathrm{O}-\mathrm{C}(3)$ |
| $P_{\text {IIf }}$ |  | 0.11 | 0.10 | 0.10 | 0.11 | 0.13 |

${ }^{a}$ Estimated error on the rotamer populations is $\pm 10 \%$.
(Table 2) for 2 PPG at pH 5.0 together with the data in Table 3 in equation (6), which together with the data from lactic acid $\left(2 J_{\mathrm{CH}^{g}}+J_{\mathrm{CH}}{ }^{t}=11.1 \mathrm{~Hz}\right)$, yields

Table 3
${ }^{13} \mathrm{C}-{ }^{1} \mathrm{H}$ and ${ }^{13} \mathrm{C}-{ }^{31} \mathrm{P}$ coupling constants ${ }^{a}$ and ${ }^{13} \mathrm{C}$ chemical shifts ${ }^{a}$ for 2 PPG and 3 PPG

|  |  |  | 2 PPG |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | pH | 1.0 | 2.8 | 5.0 | 10.8 | 1.0 | 2.8 | 4.7 | 9.8 |
| ${ }_{3}^{2} \mathrm{JO}(1) \mathrm{m}$ |  |  |  | $-3.7{ }_{0}$ |  |  |  | $-3.8{ }_{6}$ |  |
| ${ }^{3} J_{\text {O(1) }}$ |  |  |  | $0.20{ }^{\text {b }}$ |  |  |  | $1.0{ }^{\text {c }}$ |  |
| ${ }^{3}{ }^{3} \mathrm{O}(1) \mathrm{B}$ |  |  |  | 6. $0_{0}{ }^{\text {b }}$ |  |  |  | $4.8{ }_{7}{ }^{\text {e }}$ |  |
| $J_{\text {c(1) }}$ |  | 4.40 | 4.64 | 4.15 | $6.5{ }_{9}$ | 0.00 | 0.00 | 0.00 | 0.00 |
| $J_{\text {c(2) }}$ |  | $-5.1{ }^{\text {d }}$ d | $-5.1{ }_{3}{ }^{\text {d }}$ | $-5.88_{6}{ }^{\text {a }}$ | $-4.88_{8}{ }^{\text {d }}$ | $8.0{ }_{6}$ | 7.8 | $8.0{ }_{6}$ | $7.0{ }_{\text {s }}$ |
| $J_{\text {C(3) }}$ |  | 5.13 | 5.13 | $5.1{ }_{3}$ | 2.44 | $-4.8{ }_{8}{ }^{\text {d }}$ | $-4.88_{9}{ }^{\text {d }}$ | $-5.1{ }_{3}{ }^{\text {d }}$ | $-4.6{ }_{4}{ }^{\text {d }}$ |
| $\delta_{\text {O(1) }}$ |  | $173.8{ }_{1}$ | $175.0{ }^{\text {g }}$ | 177.45 | $178.9{ }^{2}$ | 175.49 | 176.49 | 178.59 | $179.5{ }_{5}$ |
| $\delta_{\text {O(2) }}$ |  | 75.93 | 76.23 | 77.95 | 77.08 | 70.92 | 71.65 | 73.0 | $73.8{ }^{\text {o }}$ |
| $\delta_{\text {O(3) }}$ |  | 63.48 | $63.8{ }_{4}$ | 64.58 | 65.60 | 67.9 | 67.85 | $68.5{ }_{9}$ | 67.5 。 |

${ }^{a}$ Coupling constants in Hz ; chemical shifts in p.p.m. to high frequency of external $\mathrm{Me}_{4} \mathrm{Si}$ from analysis of $90.5 \mathrm{MHz}{ }^{13} \mathrm{C}$ spectra [except for $\mathrm{A}, \mathrm{B}, \mathrm{M}, \mathrm{P}$ couplings to $\mathrm{C}(\mathrm{I})$ at pH 5.0 , this ${ }^{13} \mathrm{C}$ spectrum at 50.3 MHz ]. $b, \boldsymbol{c}$. The $\mathrm{C}(1) \mathrm{A}$ and $\mathrm{C}(1) \mathrm{B}$ couplings may be interchanged. ${ }^{d}$ These two-bond couplings are assumed negative.
where $J_{\mathrm{CH}^{t}}$ and $J_{\mathrm{CH}^{g}}$ are values for the trans- and gauche-vicinal ${ }^{13} \mathrm{C}^{-1} \mathrm{H}$ couplings obtained from a model system, for which we have selected lactic acid (IV).

The single resonance ${ }^{13} \mathrm{C}$ spectrum of the carboxy-

* In the analysis, calculated ${ }^{13} \mathrm{C}(1)$ band shapes are independent of the assignment between ${ }^{3} J_{\mathrm{C}(1) \mathrm{A}}$ and ${ }^{3} J_{\mathrm{C}(1) \mathrm{B}}$. However this does not affect the subsequent analysis since only the sum $J_{\mathrm{C}(1) \mathrm{A}}+J_{\mathrm{C}(1) \mathrm{B}}$ is used.
$J_{\mathrm{CH}^{g}}-11.3$ and $J_{\mathrm{CH}^{t}} 33.0 \mathrm{~Hz}$. Interchanging the values for $P_{\text {Ia }}$ and $P_{\text {te }}$ (Table 2) in equation (2), with the lactic

$$
\begin{equation*}
6.20=1.36 J_{\mathrm{CH}^{g}}+0.64 J_{\mathrm{CH}^{t}} \tag{6}
\end{equation*}
$$

acid data yields $J_{\mathrm{CH}^{g}} 5.6$ and $J_{\mathrm{Cr}^{t}}-0.06 \mathrm{~Hz}$. A similar treatment for 3 PPG at pH 4.7 yields $J_{\mathrm{CH}^{\prime}} 0.0$ and $J_{\mathrm{CH}}{ }^{t} 11.1 \mathrm{~Hz}$ for the populations as shown in Table 2,
or $J_{\mathrm{CH}^{g}} 5.6$ and $J_{\mathrm{CH}^{t}}{ }^{t} 0.0 \mathrm{~Hz}$ on interchanging the values for $P_{1 \mathrm{Ia}}$ and $P_{\mathrm{IIc}}$.

For $\alpha$-amino-acids Feeney and his co-workers ${ }^{2}$ have estimated $J_{\mathrm{CH}^{g}} 1.0 \pm 1.0$ and $J_{\mathrm{CH}^{t}} 10.6 \pm 2.0 \mathrm{~Hz}$, and adopt the criterion that $J_{\mathrm{CH}^{t}}{ }^{t}>J_{\mathrm{CH}^{g}}$. Clearly the first solution for 3 PPG, with the populations as given in Table 2, is the correct one. For 2PPG the situation is not so clear-cut, for while the first solution gives $J_{\mathrm{CH}^{t}}>J_{\mathrm{CH}^{g}}$, the magnitudes of the couplings are too large. However, values for $J_{\mathrm{CH}^{g}}$ and $J_{\mathrm{CH}^{t}}{ }^{t}$ obtained from this analysis for 2 PPG are very sensitive to small changes in the populations $P_{1 i}$. For example, if the populations shown in Table 2 were changed slightly to $P_{1 a} 0.41, P_{\mathrm{Ib}} 0.47, P_{\text {Ic }}$ 0.12 then wia equation (2) we obtain $J_{\mathrm{CH}^{g}}-1.5$ and $J_{\mathrm{Cn}^{t}} 14.0 \mathrm{~Hz}$, or on interchanging the values for $P_{1 a}$ and $P_{\mathrm{Ic}}, J_{\mathrm{CH}^{g}} 5.6$ and $J_{\mathrm{Cu}^{t}}-0.1 \mathrm{~Hz}$. Thus the solution with $P_{\mathrm{I} a}>P_{\mathrm{Ic}}$ is more reasonable, and the populations are as


PId

$P_{\text {If }}$

${ }^{P}$ Пe

${ }^{P}$ पf

Figure 3 Staggered rotamers about $\mathrm{O}-\mathrm{C}(2)$ and $\mathrm{O}-\mathrm{C}(3)$ available to $D-(+)-2 P P G$ and $D-(-)-3 P P G$, respectively
given in Table 2 as is the assignment of $\mathrm{H}_{\mathrm{A}}$ to lower frequency of $\mathrm{H}_{13}$ (Table 1).

The Conformations about the $\mathrm{C}-\mathrm{OPO}_{3} \mathrm{H}_{2}$ Bond.Sufficient coupling constant data $\left({ }^{3} J_{\mathrm{HP}},{ }^{3} J_{\mathrm{CI}}\right)$ are available from the ${ }^{1} \mathrm{H}$ and ${ }^{13} \mathrm{C}$ spectra of 2 PPG and 3 PPG to perform an analysis of the conformation about the $\mathrm{C}-\mathrm{OPO}_{3} \mathrm{H}_{2}$ bond in the manner described above for the $\mathrm{C}(2)-\mathrm{C}(3)$ bond. Here the rotamers to be considered are $P_{\mathrm{Id}-\mathrm{f}}$ for 2 PPG and $P_{\mathrm{II}-\mathrm{df}}$ for 3 PPG [see Figure 3 for projections along the $\mathrm{O} \longrightarrow \mathrm{C}(2)$ and $\mathrm{O} \rightarrow \mathrm{C}(3)$ bonds respectively].

The analysis for the rotamer populations about the $\mathrm{O}^{-} \mathrm{C}$ bonds follows that for the $\mathrm{C}(2)-\mathrm{C}(3)$ bond, with the advantage that for 2 PPG the question of the ambiguity in the assignment between $\mathrm{H}_{\mathrm{A}}$ and $\mathrm{H}_{\mathrm{B}}$ does not arise, and the assignment has already been made for 3 PPG. The relevant equations for 2 PPG are of the form (7).

$$
\begin{align*}
{ }^{3} J_{\mathrm{C}(3) \mathrm{P}} & =P_{\mathrm{Id}} J_{\mathrm{CP}^{g}}+P_{\mathrm{Ie}} J_{\mathrm{CP}} g+P_{\mathrm{If}} J_{\mathrm{CP}}{ }^{t} \\
{ }^{3} J_{\mathrm{HMP}} & =P_{\mathrm{Id}} J_{\mathrm{HP}}+P_{\mathrm{Ie}} J_{\mathrm{HP}}+P_{\mathrm{If}} J_{\mathrm{HP}} \\
1 & =P_{\mathrm{Id}}+P_{\mathrm{Ie}}+P_{\mathrm{If}} \tag{7}
\end{align*}
$$

Clearly values for the gauche- and trans- ${ }^{13} \mathrm{C}_{-}{ }^{31} \mathrm{P}$ and gauche- and trans- ${ }^{1} \mathrm{H}^{-31} \mathrm{P}$ couplings are required. In extensive studies on the conformational analysis of the amino-acids phosphoserine and phosphothreonine in aqueous solutions, Ziessow and his co-workers ${ }^{6}$ have employed the values $J_{\mathrm{CP}^{g}} 1.0$ and $J_{\mathrm{CP}^{t}} 10.0 \mathrm{~Hz}$ (after Mantsch and Smith ${ }^{7}$ ) and $J_{\mathrm{IIP}}{ }^{g} 2.5$ and $J_{\mathrm{IIP}}{ }^{t} 27.9 \mathrm{~Hz}$ (after Donaldson and Hall ${ }^{8}$ ). We use these same values, which together with experimental vicinal ${ }^{1} \mathrm{H}-{ }^{31} \mathrm{P}$ and ${ }^{13} \mathrm{C}-{ }^{31} \mathrm{P}$ couplings (Tables 1 and 3 ) in equations ( 3 ) yield the rotamer populations $P_{\text {Id-f }}$ shown in Table 2. The experimental values for the vicinal couplings ${ }^{13} \mathrm{C}(1)-{ }^{31} \mathrm{P}$ were not employed in the rotamer population analysis since the values for $J_{\mathrm{CP}^{g}}$ and $J_{\mathrm{CP}}{ }^{t}$ used above related to $s p^{3}$ lyybridised carbons and the possibility exists that different values for the gauche- and trans-couplings would be appropriate to the $s p^{2}$ hybridised C(1). However a regression analysis based upon the derived populations $P_{\text {Id-f }}$ (Table 2) and values for ${ }^{3} J_{\mathrm{C}(\mathbf{1}) \mathrm{P}}$ (Table 3) yielded $J_{\mathrm{C}(1) \mathrm{p}}{ }^{g} 2.7$ and $J_{\mathrm{C}(1) \mathrm{P}}{ }^{t} 9.1 \mathrm{~Hz}$ (correlation coefficient 0.96 ). In spite of the cumulative errors involved in this estimation these values seem entirely reasonable.

In analysing for rotamer populations about the $\mathrm{O}^{-}$ $\mathrm{C}(3)$ bond of 3 PPG it is possible to use equations analogous to (3) but based upon ${ }^{3} J_{\mathrm{H}_{A} \mathrm{P}},{ }^{3} J_{\mathrm{H}_{\mathrm{B}}}$, or ${ }^{3} J_{\mathrm{H}_{A} \mathrm{P}}$, ${ }^{3} J_{\mathrm{C}(3) \mathrm{P}}$, or ${ }^{3} J_{\mathrm{H}_{\mathrm{B}}},{ }^{3} J_{\mathrm{C}(3) \mathrm{P}}$. $\quad$ The solutions for $P_{\mathrm{IId-f}}$ of 3 PPG shown in Table 2 were obtained from the vicinal ${ }^{31} \mathrm{P}$ couplings to $\mathrm{H}_{\mathrm{A}}$ and $\mathrm{H}_{\mathrm{B}}$. Populations $P_{\text {IId-f }}$ obtained using one ${ }^{1} \mathrm{H}-{ }^{31} \mathrm{P}$ coupling and the ${ }^{13} \mathrm{C}(3)-{ }^{31} \mathrm{P}$ coupling were very similar to those given in Table 2 and did not differ by more than 0.04 in any instance.

## DISCUSSION

The rotamer populations in 2 PPG and 3 PPG may be influenced by several factors. First the combination of steric, dipolar, and electrostatic repulsion, this last being more important at higher pH values. This might be expected to destabilise $\mathrm{C}(2)-\mathrm{C}(3)$ rotamers (Ib) (2PPG) and (IIb) (3PPG) since here the polar groups form a synarrangement. However, other factors must influence the rotamer populations since (Ib) and (IIb) contribute significantly (Table 2) at all pH values. An important factor to consider is intramolecular hydrogen bonding affecting rotamer populations, for which several schemes are possible. It is possible to form a five-membered hydrogen-bonded ring between the hydroxy-proton and the phosphate oxygen (directly bonded to carbon) which would stabilise rotamers ( Ia and b) for 2PPG and (IIa and b) for 3PPG. At low pH (below $c a .3 .6$ ) a six-
membered-ring hydrogen bond between the carboxyproton and hydroxy-oxygen (for 2PPG) or the phosphate oxygen at $\mathrm{C}(3)$ (for 3 PPG ) would stabilise ( $\mathrm{Ib}, \mathrm{c}$ ) and (IIb, c) respectively. At higher pH values for 2 PPG , a six-membered hydrogen-bonded ring is also possible between a carboxylate oxygen and hydroxy-proton in rotamers (Ib and c).

The five- and six-membered hydrogen-bonding schemes would affect the conformations about the $\mathrm{C}(2)^{-}$ $\mathrm{C}(3)$ bond directly. Additionally it is possible to form a seven-membered-ring hydrogen bond between the hydroxy-proton and a terminal phosphate oxygen which would favour rotamers (Ia and b) ( 2 PPG ) and (IIa and b) (3PPG) when in combination with suitable rotamers about the $\mathrm{C}-\mathrm{O}$ (phosphate) bond.

Inspection of molecular models indicates that the five-, six-, and seven-membered hydrogen bonds are all reasonable with the observation that with the sevenmembered ring the grouping ${ }^{-} \mathrm{O}^{-} \mathrm{H} \cdots \mathrm{O}^{-}$(phosphate) is almost linear which could make this a particuarly favourable arrangement. Such seven-membered hydro-gen-bonded ring structures have been postulated in the solution conformation of ethanolamine phosphate ${ }^{9}$ and phosphoserine ${ }^{6}$ at high pH .

Overall Conformation of $2 P P G$.-In view of the possibility of rationalising all rotamer populations about the individual $\mathrm{C}(2)-\mathrm{C}(3)$ and $\mathrm{C}-\mathrm{O}$ bonds of 2 PPG and 3 PPG in terms of steric, dipolar, or electrostatic repulsion and/or various combinations of the intramolecular

(1b and d) at pH 5.0
hydrogen bonding schemes, it is desirable to look at the overall conformation of the molecule. However for 2PPG there are no experimental data to correlate the rotamer populations about $\mathrm{C}(2)-\mathrm{C}(3)$ with those about $\mathrm{C}(2)-\mathrm{O}$. For example rotamers ( Ib and d) are significantly populated at pH 5.0 ( 52 and $25 \%$, respectively). The rotamer combination of (Ib and d) at pH 5.0 allows the formation of a seven-membered hydrogen-bonded ring.

This combination might contribute as much as $25 \%$ to the overall conformation at this pH if all rotamer (Id) is associated with (Id) and not with (Ie and f). But this combination could contribute $0 \%$ if all rotamer (Id) were distributed between (Ie and f). On this basis it is only possible to consider probable overall conformations which are simply the product of the individual rotamer populations about the $\mathrm{C}(2)-\mathrm{C}(3)$ and $\mathrm{C}(2)-\mathrm{O}$ bonds. The probabilities for these overall conformations are shown in Table 4. At pH 5.0 there are five combinations with a
probability of $\geqslant 10 \%$ and at pH 10.8 there are four such combinations. However as pointed out above, there is no experimental evidence to correlate the overall conformation of 2 PPG and we will not speculate further on this.
Overall Conformation of $3 P P G$.-The probabilities for the various rotamer combinations at pH 0.6 and 9.8 are

## Table 4

Probable contributions of the rotamer combinations to the overall conformation of 2 PPG and 3 PPG

| Rotamer combination | 2PPG pH 0.5 | pH 10.8 |
| :---: | :---: | :---: |
| (Ia, d) | 0.09 | 0.10 |
| (Ia, c) | 0.104 | 0.25 |
| (Ia, f) | 0.17 | 0.07 |
| (Ib, d) | 0.13 | 0.11 |
| (Ib, e) | 0.15 | 0.28 |
| (Ib, f) | 0.24 | 0.08 |
| (Ic, d) | 0.03 | 0.03 |
| (Ic, e) | 0.03 | 0.07 |
| (Ic, f) | 0.06 | 0.02 |
|  | $3 P P G ~ p H ~ 0.6$ | pH 9.8 |
| (IIa, d) | 0.19 | 0.37 |
| (IIa, e) | 0.04 | 0.07 |
| (IIa, f) | 0.03 | 0.07 |
| (IIb, d) | 0.45 | 0.30 |
| (IIb, e) | 0.10 | 0.06 |
| (IIb, f) | 0.07 | 0.05 |
| (IIc, d) | 0.09 | 0.06 |
| (IIc, e) | 0.02 | 0.01 |
| (IIc, f) | 0.01 | 0.01 |

shown in Table 4. These indicate that two combinations [(IIa, b) and (IIb, d)] predominate. At pH 0.6 the probability of combination (IIb, d) is $\mathbf{4 5} \%$, and this may be stabilised by the six-membered hydrogen-bonded ring involving the carboxyl proton and the five-membered ring involving the hydroxy-proton.
At higher pH , the contribution of (IIb, d) probably decreases (to $30 \%$ ) while (IIa, d) becomes more significant ( $37 \%$ ). In this conformation the ionised carboxylate and phosphate groups will have a minimum

(IIb,d) at pH 0.6

electrostatic interaction while the possible five-membered liydrogen-bonded ring is retained. For the case of 3 PPG there is one piece of experimental evidence to support a significant contribution from rotamer (IIb, d) at low
pH , which decreases at high pH . This is the observation of a four-bond coupling (Table 1) ${ }^{4} J_{\mathrm{H}_{\mathrm{MP}}}$ which has the value $1.7_{7} \mathrm{~Hz}$ at pH 0.6 , decreasing to $0.5_{7} \mathrm{~Hz}$ at pH 9.8 . The rotamer combination (IIb, d) has $\mathrm{H}_{\mathrm{M}}$ and P related by a planar $W$ path and it is generally considered ${ }^{6,10}$ that values for ${ }^{4} J_{\text {IIP }}(c a .2 \mathrm{~Hz})$ are a maximum for the transanticoplanar arrangement of the four bonds involved. As the coitribution of (IIb, d) decreases, then the magnitude of ${ }^{4} /_{\mathrm{HMP}^{\mathrm{P}}}$ should decrease, as is observed.

Conclusions.-The analysis for the rotamer populations about the $\mathrm{C}(2)-\mathrm{C}(3)$ and $\mathrm{C}(2)-\mathrm{O}$ bonds of 2 PPG at pH 5.0 and 10.8 indicates that 4 or 5 possible conformations for the molecule may be significantly populated ( $\geqslant 10 \%$ ). However in the absence of experimental evidence to correlate the rotamer populations about the individual bonds it is not possible to speculate on the various factors which may influence the conformational stability.
In the case of $3 P P G$ there is evidence ( $\left.{ }^{4} J_{\mathrm{H}_{4}{ }^{\mathrm{P}}}\right)$ to correlate the rotamers about the $\mathrm{C}(2)-\mathrm{C}(3)$ and $\mathrm{C}(3)-\mathrm{O}$ bonds and two conformations [(IIa, d) and (IIb, d)] predominate in the pH range $0.6-9.8$.

The information derived here on the conformational preferences about the $\mathrm{C}(2)-\mathrm{C}(3)$ and $\mathrm{C}-\mathrm{OPO}_{3}$ bonds for 2 PPG and 3 PPG is not sufficient to substantiate the earlier proposal ${ }^{1}$ that internal mobility in 2 PPG is more restricted than in 3 PPG. While a smaller number of combination rotamers are significantly populated ( $\geqslant 10 \%$ ) for 3 PPG than for 2 PPG , no information is available on other bond rotations within the molecule [e.g. $\mathrm{C}(1)-\mathrm{C}(2) ; \mathrm{C}-\mathrm{OH}$ etc.] and therefore it is not possible to even speculate about entropy differences between 2 PPG and 3 PPG arising from restrictions on internal mobility. A more promising approach to the problem would appear to be the study of any conformational changes occurring on binding 2 PPG and 3 PPG to the enzyme phosphoglyceromutase, through the use of ${ }^{1} \mathrm{H}$ spin-echo n.m.r.

## EXPERIMENTAL

2PPG (Boehringer) and 3PPG (Sigma) were dissolved in $\mathrm{D}_{2} \mathrm{O}(99.8 \%$; Goss Scientific Instruments) to give 0.5 m solutions. The pH of the samples was adj sted by the addition of DCl or NaOD solutions. The pH values were measured using a Corning-Eel model 7 meter. The pH values quoted in the text are the meter reading and are uncorrected.
${ }^{1} \mathrm{H}$ N.m.r. spectra ( 5 mm o.d. sample tubes) were obtained in the continuous-wave mode at 100 and 220 MHz (Varian HA-100 and HR-220 instruments) and employing the pulse-Fourier-transform technique for spectra at 270 and 360 MHz (Bruker WH-270 and WH-360 instruments). ${ }^{13} \mathrm{C}$ N.m.r. spectra ( 10 mm o.d. sample tubes) were obtained in the pulse-Fourier-transform mode at 50.2 and 90.5 MHz (Bruker WP-200 and WH-360 instruments).

For many spectra, particularly both ${ }^{1} \mathrm{H}$ and ${ }^{13} \mathrm{C}$ with $\mathrm{pH}>4$. he resonances were quite broad and in these cases
better resolution was obtained after treatment of the sample with a chelating resin (Chelex-100; Bio-Rad Laboratories) according to the procedure of Irving and Lapidot ${ }^{11}$ to remove trace paramagnetic impurities. In those ${ }^{1} \mathrm{H}$ and ${ }^{13} \mathrm{C}$ spectra, obtained with the WP-200 and WH-360 instruments the convolution-difference technique ${ }^{12}$ was employed to improve the resolution of closely spaced lines. In addition all ${ }^{1} \mathrm{H}$ spectra obtained by the pulse-Fouriertransform method employed the pre-irradiation solvent (HOD) suppression technique. ${ }^{13} \quad{ }^{1} \mathrm{H}-\left({ }^{31} \mathrm{P}\right)$ Experiments were performed with the HA-100 instrument using a doubly tuned probe; the ${ }^{31} \mathrm{P}$ frequency ( 40.5 MHz ) was generated ith a Schomandl ND $100-\mathrm{M}$ synthesiser.
Spectral analyses for coupling constants and chemical shifts were made via iterative computer simulation of the spectra using the LAOCOON ILI program ${ }^{14}$ with the ICL 1900 series computer at Queen Mary College and a more compact version of the program,* ITERCAL VIB, with a Bruker BNC-12 computer. Analyses of ${ }^{1} \mathrm{H}$ spectra run at $100,220,270$, and 360 MHz were in excellent agreement; however, only the data from analysis of the $360-\mathrm{MHz}{ }^{1} \mathrm{H}$ spectra are included in the text.

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